

Study of Turbulence Kinetic Energy Budget over Jodhpur, India

Review Article

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Abstract

Atmospheric turbulence plays an important role to understand the behavior of pollutants in lower atmosphere which has a large impact on surrounding environment. In the present paper, the one-dimensional Turbulent Kinetic Energy (TKE) budget in a steady and homogeneous condition is studied. The data from a 30m micrometeorological tower during Indian Summer Monsoon (ISM) of the year 1990 over a station Jodhpur (26.3° N, 73°E), which represents a dry convective station and situated at the eastern part of ISM trough over the Indian subcontinent, is used. The tower data is of Fast and Slow Response data. The Fast Response Data (FRD) sampled at (8 Hz) is collected at 4 m and 15 m levels whereas the Slow Response Data (SRD) sampled at (~1 Hz) is collected at six levels viz. 1, 2, 4, 8, 15 and 30m. The analysis of each component of TKE budget is done for active and non-active phases of monsoon at 4m and 15m levels. All terms of TKE budget show considerable variations at 4m levels. At 15m, the variations of term are not remarkable. It has been found that at both of the levels shear production term dominates over all other terms during active phase of monsoon while buoyancy dominates during day time at 4m level in both of phases. The buoyancy and shear terms influence mixing and transport of pollutants in the lower part of the atmosphere in day time during active and non active phases of ISM. TKE budget over Jodhpur, Kharagpur and Varanasi shows that buoyancy is not a major contributing factor during the summer monsoon season while major contributing factor is shear production.

Keywords: MONTBLEX; TKE; Buoyancy; Shear; Flux divergence; Dissipation

List of Symbols

g: Acceleration due to gravity; k: Von Korman constant; θ_v : Virtual Potential Temperature; e: Turbulent Kinetic Energy; u_* : Frictional Velocity; $u'w'$: Covariance between u' and w' ; $w'\theta'$: Covariance between w' and θ' ; z: Height; ρ : Air Density; u' : Lateral eddy; v' : Transverse eddy; w' : Vertical eddy; ϵ : TKE dissipation rate

Introduction

Increasing urban population and industrial activities causes serious air pollution problem. The pollutants emitting from stack, motor vehicles, heating and cooling systems of buildings, sudden fires, etc., can either deposit nearby source or transport to a distance depending upon the temperature and wind profile in the prevailing atmosphere. The characteristics of turbulence in the lower atmosphere control the dispersion and transport of atmospheric pollutants in the atmosphere. Therefore, TKE is one of the more important variables

in lower atmosphere for the study of atmospheric pollution. The budget of TKE is directly related to the transport of heat, moisture, and momentum in lower atmosphere through atmospheric boundary layer. The tendency of TKE is important because if TKE decreases with time, the boundary layer will be less turbulent with time where as if TKE increases with time, the boundary layer will become more turbulent with time so TKE budget behaves like a source and sink.

TKE budget comprises shear production, buoyancy production, dissipation, and the transport processes which has various applications in in boundary-layer meteorology [1-3]. Panofsky [4] and Record and Cramer [5] have been studied evolution of TKE in Atmospheric Surface Layer (ASL) and found that divergence of TKE flux is important under steady condition. Busch and Panofsky [6] examined spectral characteristics of atmospheric turbulence stressed on the importance of TKE flux and found that dissipation compensates shear and buoyancy productions. Wyngaard and Cote [7] studies on

$$\bar{e} = \frac{1}{2}(\overline{u'^2} + \overline{v'^2} + \overline{w'^2})$$

The first term is the buoyant production term, which is usually a source/sink during day/night time. The second term is shear production of TKE, which is always source. The third is the divergence of vertical flux of turbulent kinetic energy, which can be a source or sink depending upon whether TKE flows into or going away from the layer. The fourth is turbulent transport of TKE by pressure fluctuations, which can again be a source/sink. The last term is dissipation, which is always a sink. Since data on pressure fluctuation are not available so pressure transport term is treated as residual term. The buoyancy and shear terms computed with the help of FRD and SRD. The vertical transport term is computed by following relation given by Mc Bean and Elliot [9].

A non dimensional form of equation (1) can be obtained by scaling it with $u_*'^3/kz$, so

$$\begin{aligned} \phi_m(z/L) - z/L - (kz/u_*'^3) \partial(\overline{w'e})/\partial z - \\ (kz/u_*'^3) \rho \partial(\overline{w'p})/\partial z - \epsilon \epsilon = 0 \end{aligned} \tag{2}$$

The vertical transport can be written as,

$$\frac{kz}{u_*'^3} \frac{\partial(\overline{w'e})}{\partial z} = \frac{kz}{L} \frac{\partial(\overline{w'e}/u_*'^3)}{\partial(z/L)} \tag{3}$$

Since $\left(\frac{\overline{w'e}}{u_*'^3}\right)$ is a universal function of z/L ,

$$\text{So taking, } \frac{\overline{w'e}}{u_*'^3} = F(z/L)$$

This function is obtained by a least square method with number of runs. It is differentiated with z/L and multiplied by $u_*'^3/L$ to get for each of the runs.

Finally, the flux divergence becomes

$$\begin{aligned} \frac{kz}{u_*'^3} \frac{\partial(\overline{w'e})}{\partial z} &= \frac{kz}{L} \frac{\partial\{F(z/L)\}}{\partial(z/L)} \\ \text{or, } \frac{\partial(\overline{w'e})}{\partial z} &= \frac{u_*'^3}{L} \frac{\partial(F(z/L))}{\partial(z/L)} \end{aligned} \tag{4}$$

For near neutral conditions,

$$\epsilon = (u_*'^3/kz) \left[1 + 0.5 \left(|z/L|\right)^{2/3}\right]^{2/3}$$

For stable conditions,

$$\epsilon = (u_*'^3/kz) \left[1 + 2.5 \left(|z/L|\right)^{3/5}\right]^{3/2}$$

In the present study, the dissipation term is computed by following Stull [22]. The pressure transport term was computed as residual, which is likely to contain any possible errors in all the remaining terms of TKE budget.

Results and Discussions

The buoyancy, shear and flux divergence of TKE budget are averaged for day time, mean of whole day and night time for the periods of active and non active respectively. The mixing and transport of pollutants depends on relative magnitudes of buoyancy and shear terms and flux divergence, mainly. The dissipation and residual terms of TKE budget do not have significant role in dispersion of atmospheric pollutants, therefore these two terms are not considered here.

Buoyancy

The buoyancy represents the generation or destruction of TKE by vertical flux of virtual potential temperature. In general, buoyancy remains positive at lower atmospheric level and decreases approximately linearly with height up to the top of the mixed layer. Hence, this term will be larger during day time and smaller or negative during cloudy days or night time. The variation of buoyancy at 4m and 15 m in day time, mean of whole day and night time during active and non active phases is shown in Figures 1a and 1b. At 4m level, during active phase (Figure 1a), the buoyancy is positive during day time while it is negative in night time but the difference between two levels during day time is more in compare to non active phase (Figure 1b). It seems that less cloudy days and clear sky during non active phase are more convective and therefore more buoyancy is found. Although the difference of buoyancy at two levels (4 and 15m) during night time in active phase is relatively large that that of non active phase. It seems that buoyancy is dominating during day time in non active phase. More buoyancy at lower level would lead more convective condition and therefore more pollutants can be dispersed in the vertical atmosphere.

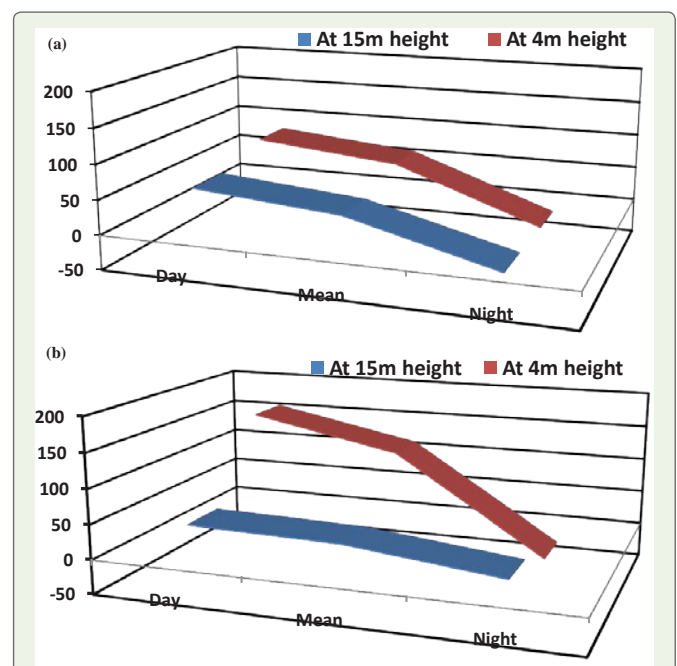


Figure 1: Buoyancy(x10⁻⁵) (m²s⁻²) in TKE budget at 4m and 15 heights in day time, mean and night time during (a) active; (b) non active phases.

Shear

In TKE budget, shear is the interaction of the turbulent momentum flux with the mean vertical wind shear that generates turbulence. This term remains generally very large and positive near the ground and becomes larger on a windy day (larger vertical shear) and smaller on a calm day. This term shows the production of eddies by shear. The wind near the ground is generally stronger than the shear at slightly higher level. During day time, the shear is also found more than at night. Figures 2a and 2b depicts the variation of shear in day time, mean of whole day and night time at 4 and 15m during active and non active phases. At 4m level, the mean values of wind shear are more in compare to its value at 15m in active and non active phases (Figures 2a and 2b) although its values are found more in active phases due to windy condition, in compare to non active phase at corresponding level. If the source of atmospheric pollutants over this area exists, the large wind shear at 4m level will disperse or transfer pollutants, which are remaining in the lower level, in the vertical atmosphere. At each level and their phases, the day time shear is found more with respect to night time, except in active phase at 15m level, and therefore dispersion of pollutants could be more in the vertical atmosphere.

Flux divergence

The flux divergence term in TKE budget represents the vertical transport of TKE. Since it shows the flux divergence of TKE for a layer since it depends on the vertical gradient of vertical flux. So, for a given layer, if more flux in entering the layer than leaving it, there would be net convergence of the vertical flux, and therefore, the TKE of the layer will increase which may carry more pollutants in the vertical atmosphere. Figure 3a and b represents the variation of flux

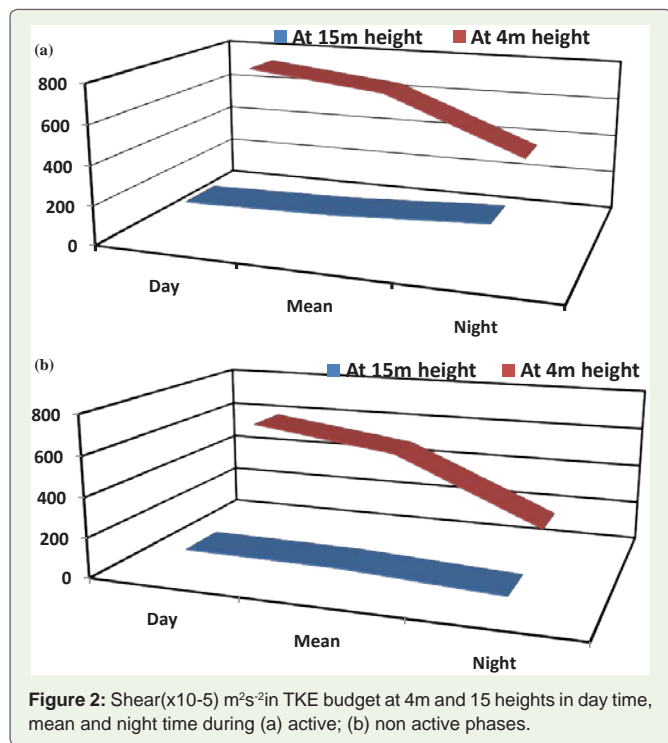


Figure 2: Shear(x10-5) m²s⁻²in TKE budget at 4m and 15 heights in day time, mean and night time during (a) active; (b) non active phases.

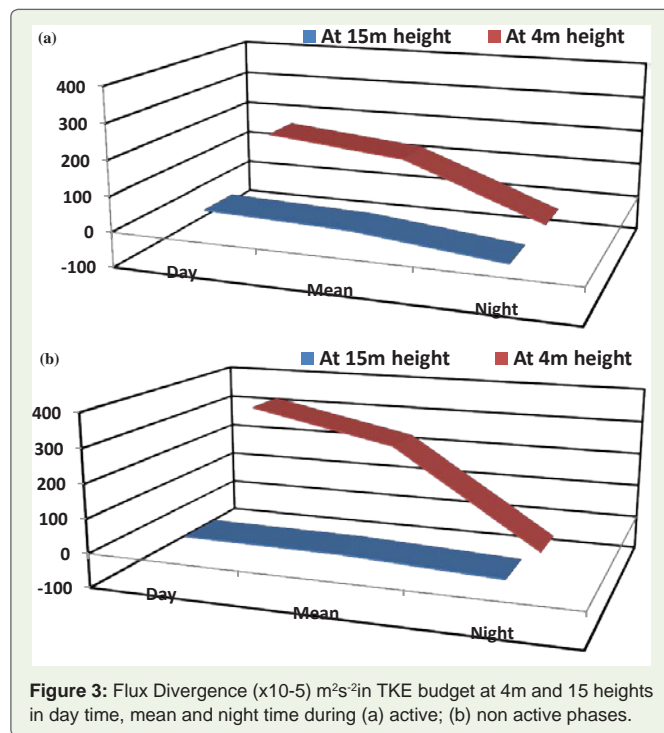


Figure 3: Flux Divergence (x10-5) m²s⁻²in TKE budget at 4m and 15 heights in day time, mean and night time during (a) active; (b) non active phases.

divergence at 4 and 15m levels in day time, mean of whole day and night time during active and non active phases respectively. In active phase (Figure 3a), the flux divergence seems to more during day time at 4m with respect 15m and therefore more turbulence in entering in the layer 4-15m during day time which in turn will increase TKE in the layer. It will lead to more dispersion of pollutants during day time in compare to night time. In non active phase (Figure 3b), the shear is found more at 4m level that that of 15m level during day time while the night time values are less. Therefore, the atmospheric pollutants will settled down during night times which have been dispersed more during day time period in the layer 4-15m. In both of the figs, more turbulence is entering during day time in compare to night time but entering of TKE in layer 4-15m is large in non active phase with respect to active phase.

Comparison of TKE Budget over Jodhpur, Varanasi and Kharagpur

Tables 4 and 5 show magnitude of the budget terms for three stations namely Jodhpur, Kharagpur and Varanasi at 15m level during active and nonactive phases. The magnitude of buoyancy term over Jodhpur is more followed by Kharagpur and Varanasi, respectively. During active phase, buoyancy at Varanasi is comparable with Jodhpur. In non active phase, buoyancy is more over Jodhpur followed by Kharagpur and Varanasi. The magnitude of shear production is highest over Kharagpur during non active phase and over Jodhpur during active phase. The flux divergence shows transport of TKE away over Kharagpur while it is brought over Varanasi and Jodhpur over both phsases. The maximum transport of TKE is noticed over Jodhpur followed by Varanasi and Kharagpur.

Table 4: TKE budget parameters during active phase at 15m height over Jodhpur (26.3°N, 73°E), Varanasi (25.2°N, 82.9°E) and Kharagpur (22.3°N, 87.3°E).

Periods	Averaged synoptic conditions
2 nd -8 th August, 1990	Sky was partially or completely cloud. Rain was continuing almost whole day Windy condition prevailed.
9 th -15 th August, 1990	Sky was either clear or partially cloudy during whole day. Wind was mild.

Table 5: TKE budget parameters during non active phase at 15m height over Jodhpur (26.3°N, 73°E), Varanasi (25.2°N, 82.9°E) and Kharagpur (22.3°N, 87.3°E).

Stations	TKE Budget		
	Buoyancy	Shear	Flux Divergence
Jodhpur	38.5	109.3	30.8
Varanasi	-5.3	181.2	-3.6
Kharagpur	26.3	267.9	-6.1

Conclusions

The study of turbulence in the atmosphere over Jodhpur helps to understand the behavior of particulate matter during monsoon season. The analysis concludes that buoyancy, shear and flux divergence of TKE budget plays significant role for the dispersion of atmospheric pollutants. The buoyancy values in mean of whole day and day time are more during non active phase at corresponding levels with respect to active phase. More buoyancy at lower level will lead more convection and therefore more pollutants can be dispersed in vertical atmosphere. Buoyancy during day time acts as source where as it behaves as sink during night time. The shear of TKE budget, at 4m level, shows that wind shear during day time is more in compare to its value at 15m in active and non active phases although its values are found more in active phases which may be due to windy condition, in compare to non active phase at corresponding level. If the source of atmospheric pollutants exists nearby by Jodhpur station, the large wind shear at 4m level will disperse or transfer pollutants remaining in the lower level, in the vertical atmosphere. In the layer 4-15m, flux divergence of TKE budget is entering more during day time in non active phase at corresponding time in active phase. Therefore, the atmospheric pollutants will settled down during night times, which has been dispersed more during day time period in the layer 4-15m. The study of relative magnitudes of buoyancy, shear and flux divergence at 4 and 15m in day and night time during active and non active phases over Jodhpur can be correlated with the vertical mixing and transport of pollutants in vertical atmosphere near the earth surface.

From the comparison of TKE budget over Jodhpur, Kharagpur and Varanasi, it is clear that buoyancy is not a major contributing factor during the summer monsoon season. The major contributing factor is shear production. Therefore, transport of pollutants may be influenced by shear production over these stations during active and non active phases.

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References

- Han et al. (2000) An estimation of turbulent kinetic energy and energy dissipation rate based on atmospheric boundary layer similarity theory.
- Holzäpfel F, Robins RE (2004) Probabilistic two-phase aircraft wake-vortex model: application and assessment. *Journal of Aircraft* 41: 1117-1126.
- Frech M (2007) Estimating the turbulent energy dissipation rate in an airport environment. *Boundary-Layer Meteorology* 123: 385-393.
- Panofsky HA, Mares E (1968) Recent measurements of cospectra of heat flux and stress. *Quart J Roy Meteor Soc* 94: 581-585.
- Record FA, Cramer HE (1966) Turbulent energy dissipation rates and exchange processes above a non-homogeneous surface. *Q J R Meteorol Soc* 92: 519-532.
- Busch NE, Panofsky HA (1968) Recent spectra of atmospheric turbulence. *Q J R Meteorol Soc* 94: 132-148.
- Wyngaard JC, Cote OR (1971) The budget of turbulent kinetic energy and temperature variance in the atmospheric surface layer. *J Atmos Sci* 28: 199-201.
- McBean GA, Miyake M (1972) Turbulent transfer mechanism in the atmospheric surface layer. *Q J R Meteorol Soc* 98: 383-398.
- McBean GA, Elliott JA (1975) The vertical transports of kinetic energy by turbulence and pressure in the boundary layer. *J Atmos Sci* 32: 753-766.
- Lenschow DH (1974) Model of the height variation of the turbulence kinetic energy budget in the unstable planetary boundary layer. *J Atmos Sci* 31: 465-474.
- Champagne FH, Friehe CA, LaRue JC, Wyngaard JC (1977) Flux measurements, flux estimation techniques and fine scale turbulence measurements in the unstable surface layer over land. *J Atmos Sci* 34: 515-530.
- Caughey SJ, Wyngaard JC (1979) The Turbulence Kinetic Energy Budget in Convective Conditions. *Quart J R Meteorol Soc* 105: 231-239.
- Viswanatham DV, Satyanarayana ANV, Mishra S, Partha Sarthi P (1997) Turbulent kinetic energy budget parameter over Varanasi from MONTBLEX-90. *Proc Indian Natl Sci Acad* 63: 403-412.
- Srivastava MK, Parth Sarthi P (2002) Turbulent kinetic energy in the atmospheric surface layer during the summer monsoon. *Meteorol Appl* 9: 239-246.
- Dacre HF, Gray SL, Belcher SE (2007) A case study of boundary layer ventilation by convection and coastal processes. *Journal of Geophysical Research*. 112: 1-18.
- Bhishma Tyagi, Satyanarayana ANV (2013) The Budget of Turbulent Kinetic Energy during Premonsoon Season over Kharagpur as Revealed by STORM Experimental Data. *ISRN Meteorology* 2013: 1-11.
- Sikka DR, Narasimha R (1995) Genesis of the Monsoon Trough Boundary Layer Experiment (MONTBLEX). *Proc Indian Acad Sci (Earth Planet Sci)* 104: 157-187.
- Srivastav SK (1995) Synoptic meteorological observations and weather condition during MONTBLEX-90. *Proc Indian Acad Sci (Earth Planet Sci.)* 104: 189-220.
- Rudrakumar S, Ameenulla S, Prabhu A (1995) MONTBLEX tower observations: Instrumentation, data acquisition and data quality. *Indian Acad. Sci. (Earth Planet Sci.)* 104: 221-248.
- Kailash KV, Malti Goel (1995) Planning MONTBLEX- An overview. The monsoon trough boundary layer, I. I. Sc. Bangalore, India.
- Kolmogorov AN (1941) Energy dissipation in locally isotropic turbulence. *Doklady AN SSSR* 32: 19-20.
- Stull, Roland B (1988) An introduction to boundary layer meteorology. Kluwer Academic Publishers, The Netherlands.

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